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AUTHOR(S):

SAKURAI, Kouichi; SHIZUYA, Hiroki

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A Complexity Theoretic Approach to Breaking Cryptosystems Based on Discrete Logarithms[†]

九州大学 櫻井 幸一 東北大学 静谷 啓樹
Kouichi SAKURAI[‡] Hiroki SHIZUYA[§]

Abstract

We investigate the complexity of breaking cryptosystems of which security is based on the discrete logarithm problem. We denote the algorithms of breaking the Diffie-Hellman's key exchange scheme by DH, the Bellare-Micali's non-interactive oblivious transfer scheme by BM, the ElGamal's public-key cryptosystem by EG, the Okamoto's conference-key sharing scheme by CONF, and the Shamir's 3-pass key-transmission scheme by 3PASS, respectively. We show a relation among these cryptosystems that

$$3PASS \leq_m^p \text{CONF} \leq_m^p \text{EG} \equiv_m^p \text{BM} \equiv_m^p \text{DH},$$

where \leq_m^p denotes the polynomial-time many-to-one reducibility. We further gives some condition in which these algorithms have equivalent difficulty. Namely,

1. If the complete factorization of $p-1$ is given, i.e. if the discrete logarithm problem is a certified one, then these cryptosystems are equivalent with respect to expected polynomial time Turing reducibility.
2. If the underlying group is the Jacobian of an elliptic curve with a prime order, then these cryptosystems are equivalent with respect to polynomial-time many-to-one reducibility.

We also discuss the complexity of several languages related to those computing problems.

[†]A detailed manuscript is available from the authors.

[‡]Department of Computer Science and Communication Engineering, Kyushu University, Hakozaki, Fukuoka 812, Japan. sakurai@csce.kyushu-u.ac.jp

[§]ECIP & GSIS, Tohoku University, Kawauchi, Aoba-ku, Sendai 980, Japan shizuya@ecip.tohoku.ac.jp